

# Implementation of a MIMO OFDM-Based Wireless LAN System

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**Abstract**—The combination of multiple-input multiple-output (MIMO) signal processing with orthogonal frequency division multiplexing (OFDM) is regarded as a promising solution for enhancing the data rates of next-generation wireless communication systems operating in frequency-selective fading environments. To realize this extension of OFDM with MIMO, a number of changes are required in the baseband signal processing. An overview is given of the necessary changes, including time and frequency synchronization, channel estimation, synchronization tracking, and MIMO detection. As a test case, the OFDM-based wireless local area network (WLAN) standard IEEE 802.11a is considered, but the results are applicable more generally. The complete MIMO OFDM processing is implemented in a system with three transmit and three receive antennas, and its performance is evaluated with both simulations and experimental test results. Results from measurements with this MIMO OFDM system in a typical office environment show, on average, a doubling of the system throughput, compared with a single antenna OFDM system. An average expected tripling of the throughput was most likely not achieved due to coupling between the transmitter and receiver branches.

**Index Terms**—MIMO systems, orthogonal frequency division multiplexing (OFDM), space division multiplexing, synchronization, wireless LAN.

## I. INTRODUCTION

THE MAIN goals in developing next-generation wireless communication systems are increasing the link throughput (bit rate) and the network capacity. Important improvements in throughput can be achieved when multiple antennas are applied at both the transmitter and receiver side, especially in a rich scattering environment. This has been shown for wireless communication links in both flat-fading [1] as well as frequency-selective fading channels [2].

Multiple-transmit multiple-receive antenna, i.e., multiple-input multiple-output (MIMO), techniques can basically be split into two groups: space time coding (STC) [3] and space

division multiplexing (SDM) [1], [2], [4]. STC increases the performance of the communication system by coding over the different transmitter branches, whereas SDM achieves a higher throughput by transmitting independent data streams on the different transmit branches simultaneously and at the same carrier frequency. Since increasing the bit rates is our goal, we will focus on SDM algorithms in this paper.

A potential application of the MIMO principle is the next-generation wireless local area network (WLAN). The current WLAN standards IEEE 802.11a [5] and IEEE 802.11g [6] are based on orthogonal frequency division multiplexing (OFDM) [7]. A potential high data rate extension of these standards could be based on MIMO [8]. This leads to the promising combination of the data rate enhancement of SDM with the relatively high spectral efficiency and the robustness against frequency-selective fading and narrowband interference of OFDM. An advantage of wireless LAN systems is that they are mainly deployed in indoor environments. These environments are typically characterized by a richly scattered multipath. As explained in [1], this is a good condition for having a high MIMO capacity.

The goal of this paper is to prove the concept of increasing the link throughput by extending an OFDM-based system with MIMO, while focusing on the IEEE 802.11a standard. Although some publications present MIMO OFDM system design and measurements [9]–[11], a good overview of the required changes on synchronization algorithms when extending OFDM with MIMO, is, to our knowledge, still lacking in the literature. Since synchronization is an essential task for any digital communication system and required for reliable reception of the transmitted data, this paper provides an overview of the necessary changes to the preamble, time and frequency synchronization, channel estimation, and synchronization tracking. Furthermore, enhanced MIMO detection algorithms are proposed, based on per-antenna-coding (PAC) (sometimes called horizontal coding [12]) at the transmitter, i.e., PAC soft-output maximum likelihood detection (MLD) and PAC V-BLAST. Finally, to verify the proposed synchronization and detection algorithms, the bit error rate (BER) and packet error rate (PER) performance of the total implementation are evaluated both with simulations and initial measurements. The initial BER and PER measurements are performed for a number of locations in a typical office environment with a MIMO OFDM test system with three transmit and three receive antennas.

The layout of the paper is as follows. Section II describes the proposed MIMO OFDM transmitter and receiver scheme. In Section III, the MIMO OFDM signal model is defined. In

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Section IV, the implementation of the MIMO OFDM synchronization and detection algorithms are presented, and the performance is shown in Section V. Finally, conclusions are drawn in Section VI.

## II. SYSTEM DESCRIPTION

Consider a MIMO OFDM system with  $N_t$  transmit (TX) and  $N_r$  receive (RX) antennas. When the MIMO technique of spatial multiplexing is applied [8], encoding can be done either jointly over the multiple transmitter branches or per branch [12]. The latter option is chosen as the encoding scheme in this paper and is called per-antenna-coding (PAC). A transmitter scheme in which PAC is applied to MIMO OFDM, is shown in Fig. 1. Basically, the MIMO OFDM transmitter consists of  $N_t$  OFDM transmitters [13], among which the incoming bits are multiplexed, and then, each branch in parallel performs encoding, interleaving ( $\Pi$ ), QAM mapping, and  $N_c$ -point inverse discrete fourier transformation (IDFT) and adds a cyclic prefix (CP) before the final TX signal is upconverted to radio frequency (RF) and transmitted. For reliable detection, it is typically necessary that the receiver knows the wireless communication channel and keeps track of phase and amplitude drifts. To enable estimation of the wireless communication channel, the transmitter occasionally sends known training symbols. In WLANs, a preamble, which includes channel training sequences, is added to every packet. Moreover, to track the phase drift, pilot symbols are inserted into every MIMO OFDM data symbol on predefined subcarriers.

The receiver first must estimate and correct for the frequency offset and the symbol timing, e.g., by using the training symbols in the preamble. Subsequently, the CP is removed, and the  $N_c$ -point discrete fourier transformation (DFT) is performed per receiver branch. Since the MIMO algorithms that are proposed in this paper are single carrier algorithms, MIMO detection has to be done per OFDM subcarrier [8]. Therefore, the received signals of subcarrier  $i$  are routed to the  $i$ th MIMO detector to recover the  $N_t$  data signals transmitted on that subcarrier. Next, the symbols per TX stream are combined, and finally, demapping, deinterleaving ( $\Pi^{-1}$ ), and decoding are performed for the  $N_t$  parallel streams and the resulting data are combined to obtain the binary output data. Section IV-F explains how the detection and decoding block of Fig. 2 is filled in for PAC soft-decision output maximum likelihood detection (PAC SOMLD) and PAC vertical BLAST (PAC V-BLAST).

## III. MIMO OFDM SIGNAL MODEL

Given the system description of Section II, we can develop a MIMO OFDM signal model. In this paper, we will need both a time-domain and frequency-domain model, i.e., we are looking for the relation between time-domain MIMO vectors  $\mathbf{u}$  and  $\mathbf{r}$  and the frequency-domain MIMO OFDM vectors  $\hat{\mathbf{s}}$  and  $\hat{\mathbf{x}}$  of Figs. 1 and 2, respectively.

Suppose that a communication system consists of  $N_t$  TX and  $N_r$  RX antennas and is denoted as a  $N_t \times N_r$  system, where the transmitter at a discrete time instance  $\tau$  sends an  $N_t$ -dimensional complex vector  $\mathbf{u}(\tau)$ , and the receiver records an  $N_r$ -dimensional complex vector  $\mathbf{r}(\tau)$ . For the simulations

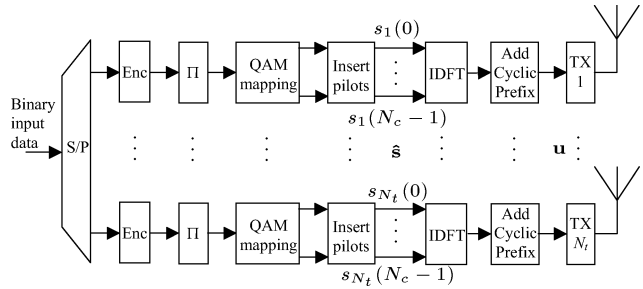


Fig. 1. Multiple-input multiple-output (MIMO) orthogonal frequency division multiplexing (OFDM) transmitter scheme.

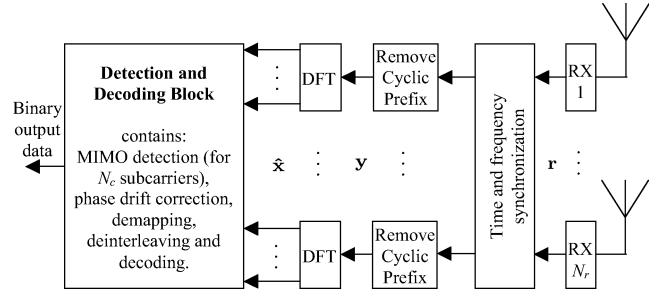


Fig. 2. MIMO OFDM receiver scheme.

in this paper, we assume that the system is operating in a frequency-selective Rayleigh fading environment and that the communication channel remains constant during a packet transmission, i.e., quasistatic fading. Suppose that the channel impulse response can be recorded with  $L$  time instances, i.e., time samples, then the fading channel between the  $p$ th TX and  $q$ th RX antenna can be modeled by a discrete-time baseband equivalent  $(L - 1)$ th-order finite impulse response (FIR) filter with filter taps  $g_{qp}(l)$ , with  $l = \{0, \dots, L - 1\}$ . We assume that these taps are independent zero-mean complex Gaussian random variables with variance  $\frac{1}{2}P(l)$  per dimension. The ensemble  $P(l)$ ,  $l = \{0, \dots, L - 1\}$  is called the power delay profile (PDP), and its total power is assumed to be normalized to  $\sigma_c^2 = 1$ , which is the average channel or propagation attenuation. Suppose  $g_{qp}(l)$  is the  $(q, p)$ th element of the matrix  $\mathbf{G}(l)$ ; then, the discrete-time MIMO baseband signal model is given by

$$\mathbf{r}(\tau) = \sum_{l=0}^{L-1} \mathbf{G}(l)\mathbf{u}(\tau - l) + \mathbf{v}(\tau) \quad (1)$$

where  $\mathbf{v}(\tau)$  represents additive white Gaussian noise (AWGN) at the  $\tau$ th sample with  $N_r$  independent and identically distributed (i.i.d.) zero-mean, complex Gaussian elements with variance  $(1/2)\sigma_v^2$  per dimension. The elements of  $\mathbf{u}(\tau)$  are assumed zero mean, uncorrelated random variables with variance  $\sigma_u^2$ . Therefore, the expected SNR per receive antenna can be shown to be  $\rho = N_t\sigma_u^2/\sigma_v^2$ . Note that, for a fair comparison, we want to keep the total TX power the same as in the single-input single-output (SISO) case. Therefore, the power per TX antenna is scaled down by a factor  $N_t$ .

To deal with the frequency selectivity of the channel, we apply OFDM, utilizing  $N_c$  subcarriers per antenna transmission. To combat inter-symbol interference (ISI), a CP of  $N_g$  samples

is added to the OFDM symbols. When  $L \leq N_g + 1$ , ISI does not occur on a MIMO OFDM symbol basis, and the  $a$ th received MIMO OFDM symbol (after removal of the CP) is given by

$$\hat{\mathbf{y}}(a) = \mathbf{C}\hat{\mathbf{u}}(a) + \hat{\mathbf{v}}(a), \quad a = 0, 1, \dots \quad (2)$$

where, with  $N_{\text{tot}} = N_g + N_c$

$$\hat{\mathbf{u}}(a) = \begin{pmatrix} \mathbf{u}(aN_{\text{tot}} + N_g) \\ \vdots \\ \mathbf{u}(aN_{\text{tot}} + N_{\text{tot}} - 1) \end{pmatrix} \quad (3)$$

$$\hat{\mathbf{v}}(a) = \begin{pmatrix} \mathbf{v}(aN_{\text{tot}} + N_g) \\ \vdots \\ \mathbf{v}(aN_{\text{tot}} + N_{\text{tot}} - 1) \end{pmatrix} \quad (4)$$

and  $\mathbf{C}$  is an  $N_c N_r \times N_c N_t$  block circulant matrix. In general, an  $NA \times NB$  matrix is called block circulant if it has the form

$$\mathbf{C} = \begin{pmatrix} \mathbf{C}_0 & \mathbf{C}_{N-1} & \mathbf{C}_{N-2} & \dots & \mathbf{C}_1 \\ \mathbf{C}_1 & \mathbf{C}_0 & \mathbf{C}_{N-1} & \dots & \mathbf{C}_2 \\ \mathbf{C}_2 & \mathbf{C}_1 & \mathbf{C}_0 & \dots & \mathbf{C}_3 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \mathbf{C}_{N-1} & \mathbf{C}_{N-2} & \mathbf{C}_{N-3} & \dots & \mathbf{C}_0 \end{pmatrix} \quad (5)$$

where the blocks, which are denoted by  $\mathbf{C}_x$ , are  $A \times B$  matrices. Note that the block circulant matrix is fully defined by its first  $NA \times B$  "block vector." In our case, this first "block of columns" is  $N_c N_r \times N_t$  dimensional and given by

$$\mathbf{K} = \begin{pmatrix} \mathbf{G}(0) \\ \vdots \\ \mathbf{G}(L-1) \\ \mathbf{0}_{N_r(N_c-L) \times N_t} \end{pmatrix} \quad (6)$$

where  $\mathbf{0}_{N_r(N_c-L) \times N_t}$  is the  $N_r(N_c-L) \times N_t$  all zeros matrix. When  $\mathbf{s}(i, a)$  represents the MIMO vector transmitted on the  $i$ th subcarrier of the  $a$ th MIMO OFDM symbol and  $s_p(i, a)$  is its  $p$ th element, i.e., transmitted on the  $p$ th TX antenna, the transmitted block of samples in the time-domain becomes

$$\hat{\mathbf{u}}(a) = (\mathbf{F}^{-1} \otimes \mathbf{I}_{N_t}) \begin{pmatrix} \mathbf{s}(0, a) \\ \vdots \\ \mathbf{s}(N_c - 1, a) \end{pmatrix} \quad (7)$$

where  $\otimes$  denotes the Kronecker product,  $\mathbf{F}$  is the  $N_c \times N_c$  Fourier matrix, of which the  $(i, k)$ th element equals  $\exp(-j2\pi(ik/N_c))$ , and  $\mathbf{I}_N$  represents the  $N \times N$ -dimensional identity matrix. Finally, by taking the DFT at the receiver, we obtain the frequency-domain MIMO OFDM baseband signal model (under the assumption that  $L \leq N_g + 1$ )

$$\begin{aligned} \hat{\mathbf{x}}(a) &= (\mathbf{F} \otimes \mathbf{I}_{N_r}) \hat{\mathbf{y}}(a) \\ &= (\mathbf{F} \otimes \mathbf{I}_{N_r}) (\mathbf{C}(\mathbf{F}^{-1} \otimes \mathbf{I}_{N_t}) \hat{\mathbf{s}}(a) + \hat{\mathbf{v}}(a)) \\ &= \hat{\mathbf{H}} \hat{\mathbf{s}}(a) + \hat{\mathbf{n}}(a) \end{aligned} \quad (8)$$

where  $\hat{\mathbf{n}}(a)$  represents the frequency-domain noise, with i.i.d. zero-mean, complex Gaussian elements with variance  $(1/2)\sigma_n^2$

per dimension, and  $\hat{\mathbf{H}}$  is a block diagonal matrix, which is given by

$$\hat{\mathbf{H}} = \begin{pmatrix} \mathbf{H}(0) & & 0 \\ & \ddots & \\ 0 & & \mathbf{H}(N_c - 1) \end{pmatrix}. \quad (9)$$

The  $i$ th block diagonal element is the  $N_t \times N_r$  MIMO channel of the  $i$ th subcarrier and can be shown to be

$$\mathbf{H}(i) = \sum_{l=0}^{L-1} \mathbf{G}(l) \exp(-j2\pi \frac{il}{N_c}). \quad (10)$$

So, for this subcarrier, we may write

$$\mathbf{x}(i, a) = \mathbf{H}(i)\mathbf{s}(i, a) + \mathbf{n}(i, a) \quad (11)$$

which results in a flat-fading signal model per subcarrier. Note that if  $N_c$  is a power of 2, the (I)DFT can be implemented efficiently with the (inverse) fast Fourier transform [(FFT)].

#### IV. IMPLEMENTATION

Synchronization is an essential task for any digital communication system and required for reliable reception of the transmitted data. From the perspective of physical layer design, proper synchronization algorithms are crucial to build a successful product. Therefore, for a potential application of MIMO to OFDM, it is important to examine the necessary changes to the preamble, time and frequency synchronization, channel estimation, synchronization tracking, and detection. Sections IV-A–F will give an overview of these necessary changes. In this evaluation, we will assume that the receiver gains (per branch) are already set by, e.g., an automatic gain control (AGC) algorithm. Since the AGC for a MIMO system does not differ significantly from the SISO case, it will not be treated in this paper.

##### A. Preamble

The radio communication system under investigation (i.e., WLAN) is a packet-switched system with a random access protocol. This essentially means that a receiver has no *a priori* knowledge about packet-arrival times. The random nature of the arrival times and the high data rates require the synchronization to be completed shortly after the start of the reception of a packet. To facilitate "quick" synchronization, the data packet is preceded with a known sequence (the preamble). The preamble is carefully designed to provide enough information for a good packet detection, frequency offset estimation, symbol timing, and channel estimation. With accurate knowledge of the MIMO channel elements, the MIMO processing can separate the signal components originating from the different transmit antennas.

To estimate the MIMO channel, it is important that the subchannels from the different TX antennas to every RX antenna can be uniquely identified. To achieve that, the preambles on the different TX antennas should be orthogonal and shift-orthogonal, for at least the channel length [14]. We have chosen for time orthogonality as shown in Fig. 3.

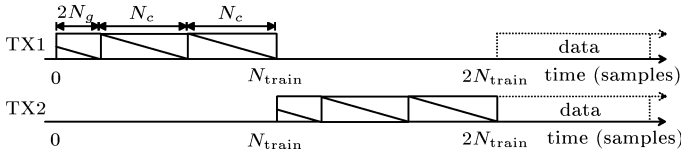


Fig. 3. Concept of a time orthogonal preamble for a MIMO configuration with two transmit antennas.

To perform frequency offset estimation, a periodicity in the preamble is desired since the phase rotation between time-delayed versions of the same symbol is a measure for the frequency offset [15]. Therefore, the proposed preamble consists of a concatenation of two identical training sequences per TX antenna.

Furthermore, to make the channel estimation less vulnerable to ISI, a CP of length  $2N_g$  is added. Altogether, this results in a preamble as depicted in Fig. 3 for a  $2 \times 2$  system. Following the IEEE 802.11a standard, the training sequence is chosen to be the standards' long training symbol, with  $N_g = 16$  and  $N_c = 64$  [5], resulting in a nonzero part per TX antenna of  $N_{\text{train}} = 2N_g + 2N_c$  samples. In the remainder of this paper, we will denote the signal on the  $i$ th subcarrier of the long training symbol by  $c(i)$ .

Note that since the total length of the proposed preamble grows linearly with  $N_t$ , it is not highly efficient. This results in an increased overhead. More efficient channel training sequences for MIMO OFDM are proposed in [14]. It is claimed that training sequences for the different transmit antennas are optimal if they are orthogonal, as well as shift orthogonal over the sampling interval  $\{-L + 1, \dots, L - 1\}$ . Since the impulse response length  $L$  is not known in advance, the simplest implementation would be to choose a fixed orthogonality interval. If the shift orthogonality is not satisfied, however, training following the design rules of [14] becomes unstable, leading to an undesirable performance degradation. Therefore, stable but efficient channel estimation algorithms remain a topic for further research.

### B. Time Synchronization

1) *Frame Detection/Coarse Timing*: The task of the frame detection (FD) is to identify the preamble in order to detect a packet arrival. This preamble detection algorithm can also be used as a coarse timing (CT) algorithm, since it inherently provides a rough estimate of the starting point of the packet. In literature different data-aided FD algorithms have been proposed for OFDM, [16]–[18]. A simple MIMO extension of Schmid's algorithm [17] was proposed in [19]. All these algorithms are based on the correlation between the repeated symbols constituting the preamble.

We define the complex correlation  $\Lambda$  between two subsequently received frames of  $N_c$  samples on the  $N_r$  receive antennas as

$$\begin{aligned} \Lambda(\tau) &= \sum_{n=\tau-(N_c-1)}^{\tau} \mathbf{r}^H(n - N_c) \mathbf{r}(n) \\ &= \sum_{n=\tau-(N_c-1)}^{\tau} \sum_{q=1}^{N_r} r_q^*(n - N_c) r_q(n) \end{aligned} \quad (12)$$

where  $H$  denotes the conjugate or Hermitian transpose, and  $r_q(\tau)$  is the  $n$ th sample of the received signal on antenna  $q$ . The sum of the power of  $N_c$  subsequently received samples on the  $N_r$  receive antennas together, denoted by  $P$ , is defined as

$$\begin{aligned} P(\tau) &= \sum_{n=\tau-(N_c-1)}^{\tau} \mathbf{r}^H(n) \mathbf{r}(n) \\ &= \sum_{n=\tau-(N_c-1)}^{\tau} \sum_{q=1}^{N_r} r_q^*(n) r_q(n). \end{aligned} \quad (13)$$

Here, we propose to use the maximum-normalized-correlation (MNC) criterion for FD, which was proposed in [18] for a SISO OFDM system and shown to perform better than techniques proposed in [16] and [17]. In the MNC frame detection algorithm, the estimated start of the datapacket, i.e., the end of the preamble, is given by

$$\tau_{\text{FD}} = \arg \max_{\tau} \left[ \frac{\sum_{p=1}^{N_t} 4|\Lambda(\tau_p)|^2}{\sum_{p=1}^{N_t} P(\tau_p - N_c)^2 + P(\tau_p)^2} \right] \quad (14)$$

where  $\tau_p = \tau - (N_t - p)N_{\text{train}}$  to consider the offset of  $N_{\text{train}}$  per TX branch (see Fig. 3). To avoid a false detection, i.e., a detection of a packet when none is present, a threshold should be set that triggers the above algorithm [20].

2) *Symbol Timing*: The symbol timing in an OFDM system decides where to place the start of the FFT window within the OFDM symbol. Although an OFDM system exhibits a guard interval (GI), making it somewhat robust against timing offsets, a nonoptimal symbol timing will cause more ISI and inter-carrier interference (ICI) in delay spread environments. This will result in a performance degradation.

The symbol timing proposed here is designed to minimize the amount of ISI and ICI that is generated in the system and is an extension of the technique proposed for SISO OFDM in [13, pp. 88–92]. Since it relies on the knowledge of the channel impulse responses (CIRs), their powers are estimated by correlating the received signals with the known training sequence

$$\begin{aligned} \eta_q(\tau) &= \left\| \sum_{k=0}^{N_c-1} r_q(\tau - k) \cdot \frac{1}{N_c} \sum_{i=0}^{N_c-1} c^*(i) e^{-j2\pi i(N_c-1-k)/N_c} \right\|^2. \end{aligned} \quad (15)$$

Subsequently, the powers of the  $N_t N_r$  impulse response estimates are summed. Note that the estimates of the powers of the CIRs, corresponding to the  $N_t$  transmitters, are spaced  $N_{\text{train}}$  samples apart in  $\eta_q$  and that  $\eta_q$  holds two estimates per TX spaced  $N_c$  samples apart, caused by the repetition in the preamble. The sum of the powers is window integrated over the length of the GI of the OFDM symbol  $N_g$ . The joint symbol timing for the whole MIMO receiver  $\tau_{\text{est}}$  is then found by

searching the maximum of the window integral, i.e., a measure for the start of the payload:

$$\tau_{\text{est}} = \arg \max_{\tau} \sum_{l=0}^{N_g-1} \sum_{p=1}^{N_t} \sum_{q=1}^{N_r} \sum_{n=0}^1 \eta_q(\tau_p - l - nN_c). \quad (16)$$

This search window should be centered around  $\tau = \tau_{\text{FD}}$ , as determined by (14).

### C. Frequency Synchronization

The frequency synchronization has to correct for the frequency offset, which is caused by the difference in oscillator frequencies at the transmitter and the receiver. We estimate this frequency offset and compensate the received signals for it. The frequency offset can be estimated using the phase of the complex correlation  $\Lambda$  between the two consecutive received training symbols, as was shown by Moose for a SISO OFDM system in [15] and further worked out in [17]. A simple MIMO extension of Moose's algorithm was proposed in [19]. Here, it is assumed that all transmit/receive branches of one MIMO transmitter/receiver use the same oscillator, which is a valid assumption if the different transmit/receive branches are co-located. The best instant to estimate this frequency offset is at timing instant  $\tau = \tau_{\text{FD}}$ . The estimated frequency offset  $\Delta f_{\text{est}}$  is then given by

$$\Delta f_{\text{est}}(\tau) = \frac{\theta_{\text{est}}(\tau)}{2\pi T_c} = \frac{f_s \angle \left[ \sum_{p=1}^{N_t} \Lambda(\tau_p) \right]}{2\pi N_c} \quad (17)$$

where  $\theta_{\text{est}}$  denotes the phase of the summation of the complex correlations  $\Lambda$  of the training symbols originating from the different transmitters,  $f_s$  equals the sample frequency,  $T_c = N_c/f_s$  is the training symbol duration and  $\angle(\cdot)$  denotes the angle (in radians) of its argument. The maximum estimated frequency offset is limited, since the angle  $\theta_{\text{est}}$  that can be estimated without phase ambiguity is limited to  $\theta_{\text{max}} = \pm\pi$ . This relates to a maximum frequency offset of  $|\Delta f_{\text{max}}| = |\theta_{\text{max}}|f_s/2\pi N_c = f_s/2N_c$ , which equals half the subcarrier spacing. A larger range can be achieved by slightly changing the preamble, as was proposed in [17]. As an accuracy measure of the estimator, we consider the normalized variance of the estimator in an AWGN channel, as was derived in [15] for the SISO estimator. The normalized variance of the MIMO estimator is given by

$$\begin{aligned} \text{var} \left( \frac{\Delta f_{\text{est}} - \Delta f}{\Delta F} \right) &= E \left( \frac{\Delta f_{\text{est}} - \Delta f}{\Delta F} \right)^2 \\ &= \frac{1}{(2\pi)^2 N_r N_c \rho} \end{aligned} \quad (18)$$

where  $\rho$  denotes the SNR per receive antenna,  $\Delta f$  the actual frequency offset, and  $\Delta F = f_s/N_c$  the subcarrier spacing. It can be shown that the variance of the estimator equals the mean squared error (MSE), since the estimator is unbiased. It is clear from (18) that the accuracy increases linearly with the number of receive antennas  $N_r$ . Note that the Cramér-Rao lower bound

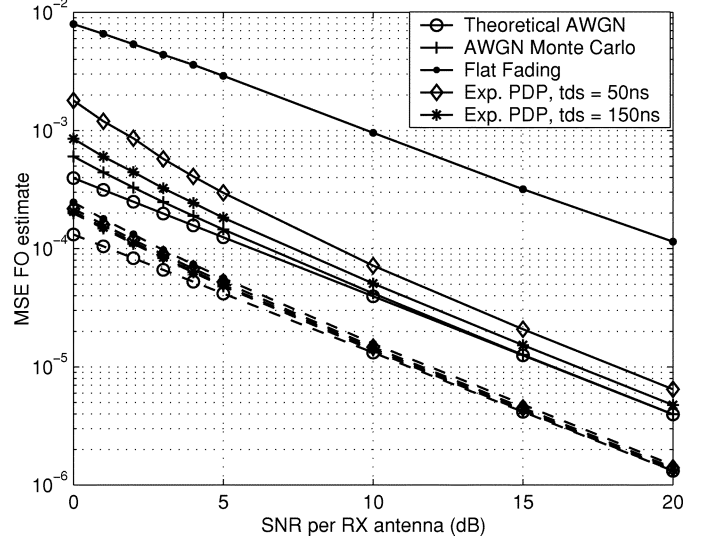


Fig. 4. MSE of the frequency offset estimate for a  $1 \times 1$  (solid lines) and a  $3 \times 3$  (dashed lines) system from theory and simulations with AWGN and multipath channels.

is equal to this theoretical value of the variance, as was already concluded for the SISO version in [17].

In Fig. 4, the MSE of the frequency offset (FO) estimation is depicted as function of the average SNR per receive antenna. The theoretical value from (18) is shown together with results from Monte Carlo simulations averaged over 100 000 channel realizations for exponentially decayed PDP having different values of rms delay spread (tds). Fig. 4 shows the results for the SISO and  $3 \times 3$  configuration. It is clear that the theoretical value is a good estimate of the MSE for high SNR values but underestimates the MSE compared with simulation results for low SNR. In case of AWGN, we see an improvement of 4.8 dB in performance going from a  $1 \times 1$  to a  $3 \times 3$  configuration, as expected from (18).

The simulations with multipath channels show a degradation in performance with respect to the theoretical and the simulated AWGN case. The degradation is the worst for the flat-fading case and decreases when the rms delay spread increases. This is explained by the frequency diversity introduced by the delay spread channel. The degradation, however, is much smaller in the  $3 \times 3$  case than in the SISO case. This shows that the frequency offset estimation in MIMO systems is more robust under different fading conditions, which can be explained by the space diversity introduced by the multiple antennas.

### D. Channel Estimation

When time synchronization is performed at the receiver and after the received signals are corrected for the frequency offset, the channel can be estimated using the known training symbols within the preamble. When the timing is performed correctly, we know which received samples correspond to the training part. More precisely, we know exactly which part of the received preamble is sent by transmit antenna  $p$  (see Fig. 3). Therefore, in the analysis of this subsection, we will omit the MIMO OFDM symbol index for brevity. Let us denote the Fourier transform

of the symbol received on antenna  $q$  that corresponds to the training symbol from transmitter  $p$  by

$$\hat{\mathbf{x}}_q^p = \begin{pmatrix} x_q^p \end{pmatrix}$$

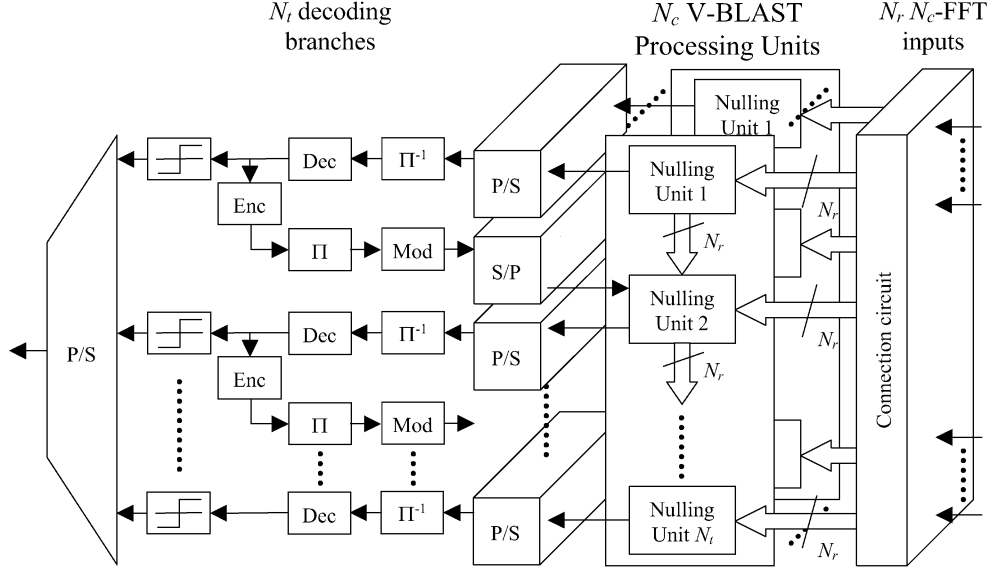


Fig. 5. PAC V-BLAST detection and decoding block.

Rayleigh channel (i.e., each subcarrier is treated flat over frequency), we know that this vector  $\mathbf{x}$  has a complex multivariate normal distribution [8]. Therefore, for a given channel matrix  $\mathbf{H}$ , the conditional probability density function can be shown to be

$$p(\mathbf{x}|\mathbf{H}, \mathbf{s}_j) = \frac{1}{\det(\pi\mathbf{Q})} \cdot e^{-(\mathbf{x}-\mathbf{H}\mathbf{s}_j)^H \mathbf{Q}^{-1}(\mathbf{x}-\mathbf{H}\mathbf{s}_j)} \quad (26)$$

where  $\mathbf{Q}$  is the covariance matrix and equals

$$\begin{aligned} \mathbf{Q} &= E[(\mathbf{x} - E[\mathbf{x}])(\mathbf{x} - E[\mathbf{x}])^H] \\ &= E[(\mathbf{x} - \mathbf{H}\mathbf{s}_j)(\mathbf{x} - \mathbf{H}\mathbf{s}_j)^H] \\ &= E[\mathbf{nn}^H] = \sigma_n^2 \mathbf{I}_{N_r}. \end{aligned} \quad (27)$$

Finally, we obtain the LLR of  $b_k$

$$\text{LLR}(b_k) = \ln \frac{\sum_{s_j | b_k = +1} \exp\left(-\frac{D}{\sigma_n^2}\right)}{\sum_{s_j | b_k = -1} \exp\left(-\frac{D}{\sigma_n^2}\right)} \quad (28)$$

where  $D = \|\mathbf{x} - \mathbf{H}\mathbf{s}_j\|^2$ . When applying the max-log approximation this results in

$$\text{LLR}(b_k) \approx \frac{1}{\sigma_n^2} \left( \min_{s_j | b_k = -1} D - \min_{s_j | b_k = +1} D \right). \quad (29)$$

Once the LLRs are computed, they are deinterleaved and decoded. Since the TX streams are encoded separately, the deinterleaving and decoding also has to be performed per stream. Hence,  $N_t$  deinterleavers and Viterbi decoders are required to produce the final output.

Note that SOMLD involves an exhaustive search over all possible vectors  $\mathbf{s}_j$ , leading to a complexity that grows exponentially with  $N_t$ .

2) *Per-Antenna-Coded V-BLAST*: The fact that the complexity of MLD grows exponentially with the number of transmit antennas resulted in the search for less com-

plex algorithms. One of the schemes that is based on minimum-mean-square-error (MMSE) detection with decision-feedback equalization (DFE) is called V-BLAST [24], [26]. The complexity of this scheme grows linearly with  $N_t$  [24], and when using the proposed optimal successive interference cancellation (OSIC) in [26], the performance degradation with respect to MLD is small compared with linear techniques like zero-forcing [4]. In this paper, we propose an extension to V-BLAST, making use of PAC at the transmitter. The idea is to first go through the decoding stage before the successive interference cancellation (SIC) is executed. In this way, forward error correcting (FEC) coding is performed on the SIC information. How this can be applied to MIMO OFDM is schematically represented in Fig. 5.

To improve the performance even more, the V-BLAST detection should produce soft-decision outputs. In order to obtain them, the estimated values of each nulling unit should not be sliced to their respective QAM points, as done in [26], but they should go through a SISO implementation, i.e., the  $1 \times 1$  version of SOMLD described above.

Note that since the SIC information is passed through a decoder and encoder stage, a disadvantage of this scheme could be its latency, but when the interleaver is small, e.g., equivalent to the size of the interleaver defined in the IEEE 802.11a standard [5], and convolutional encoding and Viterbi decoding is used, the encoder in the SIC feedback loop can start its operation as soon as the Viterbi decoder produces outputs. Then, for a limited number of transmit antennas, the latency is manageable.

## V. PERFORMANCE

### A. Simulation Results

This subsection shows the results of a number of simulations that are performed to compare the BER performance of the two PAC detection schemes described in Section IV. The main simulation parameters are based on the IEEE 802.11a standard and summarized in Table I.

TABLE I  
SIMULATION PARAMETERS, BASED ON THE  
802.11A OFDM STANDARD

System Parameter	Parameter Value
Modulation	Binary Phase Shift Keying
Bandwidth	20 MHz
Number of subcarriers $N_c$	64
Number of data subcarriers	48
Number of pilot tones	4
OFDM Symbol duration	4 $\mu$ s
Guard Interval	800 ns

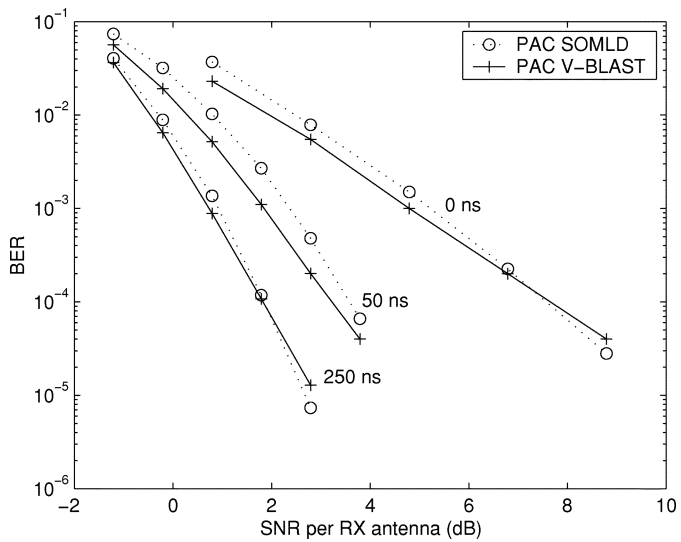


Fig. 6. BER performance for  $4 \times 4$  PAC schemes, BPSK, rate 1/2 coding, and frequency-selective Rayleigh fading with an exponential decaying PDP with



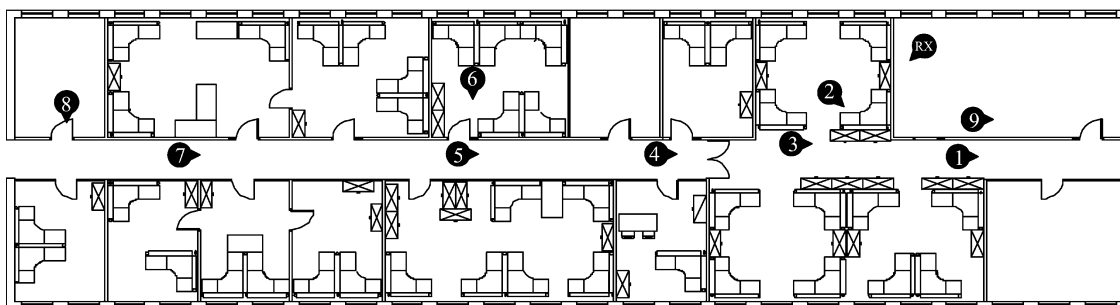


Fig. 8. Floor plan of the office where the measurements were performed (42 m  $\times$  12.7 m), including the RX and TX locations and orientations.

The baseband processing is built around two field programmable gate arrays (FPGAs) per board. In our setup, the FPGAs are mainly configured as memory banks. At the transmitter, waveforms are loaded into and sent from the memory banks, and they are recorded at the receiver. These recorded data are processed offline with software written in MATLAB to, e.g., determine the performance by means of bit errors. By transmitting multiple packets, BER tests can be performed in order to evaluate different MIMO algorithms in real-life communication channels.

### C. Comparison

Measurements with the above described test system were done in a wing on the third floor of the Agere Systems building in Nieuwegein, The Netherlands, which can be regarded as a typical office environment. The wing is 42 m  $\times$  12.7 m, and its floor plan is shown in Fig. 8. The inner walls of the wing are modular walls, whereas the rest of the walls and floors consists of concrete. Besides the walls, the desks and metal cupboards are depicted. Furthermore, the RX and nine different TX positions and orientations that were used for the measurements are shown. The applied antennas were omnidirectional, but due to obstruction by the test system, their effective patterns covered only a half plane. The antenna spacing was fixed at two wavelengths. Each transmit antenna transmitted at an average power of 50 mW. The average SNR per RX antenna and the rms delay spread that we measured per location are given in Table II. These values were measured at baseband level and, thus, include system influences. This means that the estimated rms delay spread includes the influence of filters at both transmitter and receiver. The memory of the transmitter has a storage capacity of 19 MIMO OFDM data symbols, which we always fully exploited, leading to different packet lengths for different data rates. The tested data rates and corresponding packet lengths, i.e., the number of information bits, are given in Table III. To obtain the average performance, 1000 packets were transmitted per rate. The BER and PER performance for different locations and different rates are depicted in Figs. 9–11. Note that for certain rates, no performance value is given; this corresponds to the fact that at these rates, all 1000 packets were received correctly. Furthermore, note that the  $1 \times 1$  measurements were only performed for locations 5, 6, and 7 and were obtained with the same test system by switching off two of the three boards at both TX and RX.

In Figs. 9–11, it can be observed that the performance of the  $3 \times 3$  measurements is worse than the performance of its

TABLE II  
AVERAGE SNR PER RX ANTENNA AND RMS DELAY SPREAD VERSUS POSITION

Position	Average SNR (dB)	rms delay spread (ns)
1	24	98
2	24	97
3	24	100
4	23	104
5	25	91
6	24	100
7	22	109
8	14	131
9	26	100

TABLE III  
DATA RATES AND PACKET LENGTHS

Throughput (Mb/s)	Antenna setup	Modulation	Coding Rate	Packetlength (Bytes)
6	$1 \times 1$	BPSK	1/2	57
9	$1 \times 1$	BPSK	3/4	85.5
12	$1 \times 1$	QPSK	1/2	114
18	$1 \times 1$	QPSK	3/4	171
24	$1 \times 1$	16-QAM	1/2	228
36	$1 \times 1$	16-QAM	3/4	342
48	$1 \times 1$	64-QAM	2/3	456
54	$1 \times 1$	64-QAM	3/4	513
18	$3 \times 3$	BPSK	1/2	171
27	$3 \times 3$	BPSK	3/4	256.5
36	$3 \times 3$	QPSK	1/2	342
54	$3 \times 3$	QPSK	3/4	513
72	$3 \times 3$	16-QAM	1/2	684
108	$3 \times 3$	16-QAM	3/4	1026
144	$3 \times 3$	64-QAM	2/3	1368
162	$3 \times 3$	64-QAM	3/4	1539

$1 \times 1$  counterpart with one third of the data rate. To have a PER of 1%, it can be shown that in the  $1 \times 1$  case, a rate of 54, 36, and 24 Mb/s can be achieved for locations 5, 6, and 7, respectively. For the  $3 \times 3$  case, these rates are, respectively, 108, 54, and 54 Mb/s, resulting in an average throughput enhancement of 1.92. For well-conditioned MIMO channels, i.e.,

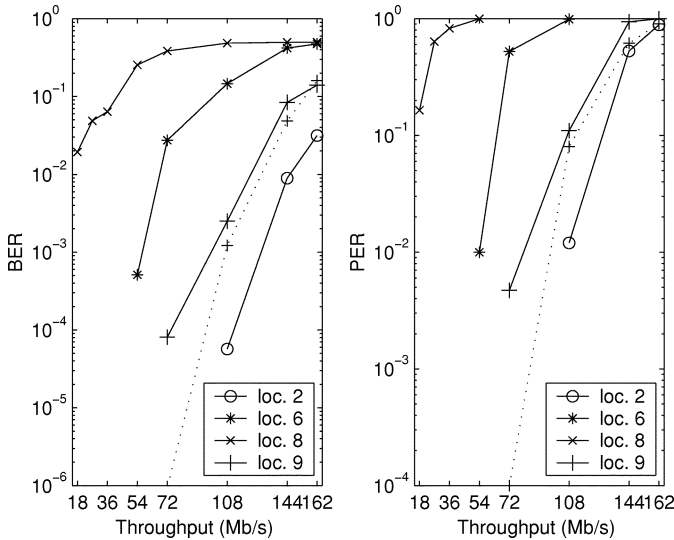


Fig. 9. Measurement results of a  $3 \times 3$  system with PAC V-BLAST detection for the TX locations 2, 6, 8, and 9. For location 9, the measurements are compared with simulations (dotted line), with an average SNR per receive antenna of 26 dB and a rms delay spread of 100 ns.

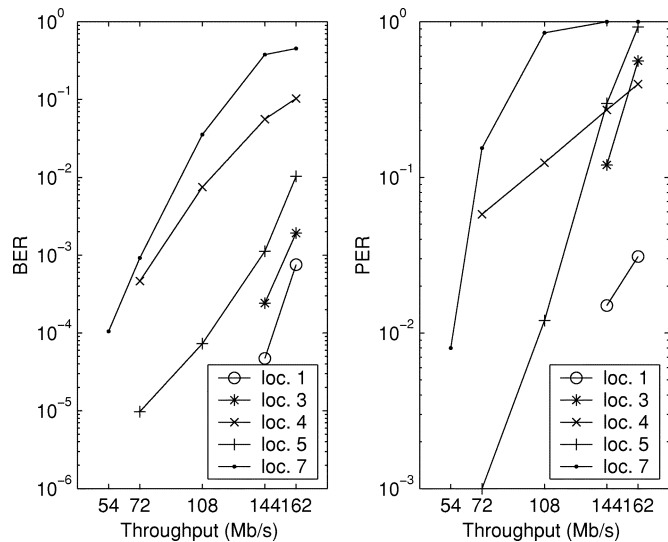


Fig. 10. Measurement results of a  $3 \times 3$  system with PAC V-BLAST detection for the TX locations 1, 3, 4, 5, and 7.

channels with i.i.d. channel elements, the throughput could theoretically be improved by a factor of 3. Clearly, the measured MIMO channels do not provide this improvement. Two arguments can explain this fact: First, the environment does not provide enough scattering, leading to ill-conditioned MIMO channels, and second, mutual coupling between the branches at the transmitter and the receiver leads to performance degradation. Since our system is not shielded very well, as can be seen from Fig. 7, the last point most likely results in the highest performance loss in our case.

Next to measurements, simulations were performed to evaluate the packet error rate (PER) performance for the  $3 \times 3$  rates 72, 108, 144, and 162 Mb/s (see Table III) and to compare the results with the measurements results. Location 9 was used for this comparison (see Fig. 8). At this position, we observed an rms delay spread of about 100 ns and an average SNR per RX

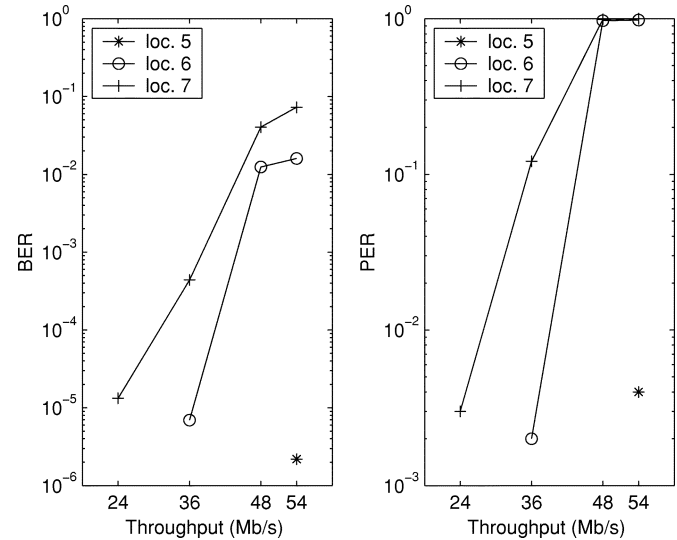


Fig. 11. Measurement results of a  $1 \times 1$  system with PAC V-BLAST detection for the TX locations 5, 6, and 7.

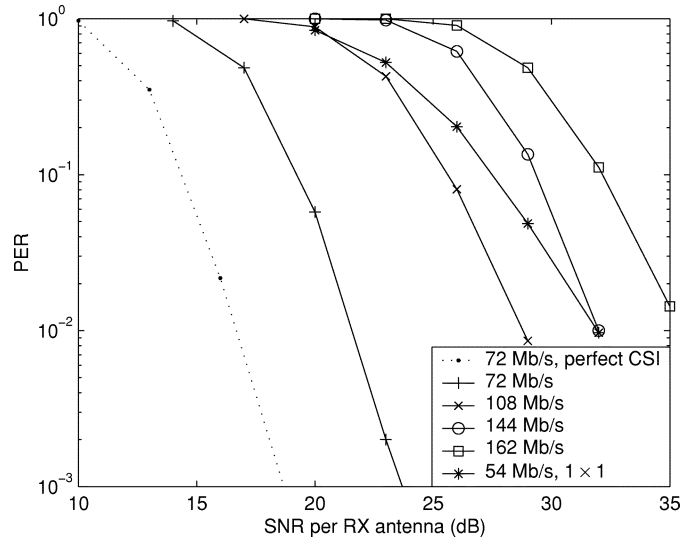


Fig. 12. PER simulation results of PAC V-BLAST for a  $1 \times 1$  and  $3 \times 3$  configuration, with perfect CSI at the receiver (dotted line) and with channel estimation (solid lines), different data rates, and frequency-selective Rayleigh fading with an exponential decaying PDP with 100 ns rms delay spread.

antenna of 26 dB. These parameters were used in the simulations. Furthermore, perfect synchronization and i.i.d. channel elements were assumed, and the PER was obtained by averaging over 10 000 packets. The results are shown in Fig. 12. All but one curve are obtained by performing channel estimation, and the other curve (based on 16-QAM modulation and coding rate 1/2) is generated assuming perfect CSI at the receiver.

From these simulation results, we see that the performance deteriorates going to higher data rates, and we observe that applying channel estimation results in a loss of more than 4 dB. A more advanced channel estimation algorithm might reduce this loss (see Sections IV-A and D). Furthermore, we note that the  $3 \times 3$  curves fall off faster than the  $1 \times 1$  curve (54 Mb/s, 64-QAM, rate 3/4 and a packet length of 513 bytes), such that at high SNRs, most of the higher MIMO rates outperform the

SISO 54 Mb/s rate, even having longer packets. This can be explained by the fact that the MIMO configurations benefit not only from the frequency diversity but from the spatial diversity as well.

Taking the simulation results at an SNR of 26 dB, we can evaluate the performance of the measurements with the test system for location 9. For different data rates and a rms delay spread of 100 ns, the results are depicted in Fig. 9 by the dotted lines. We clearly see that the performance of the test system in a real environment is worse than the performance of the idealized simulations. This can most likely be explained by system degradations that are not taken into account in the simulations, such as mutual coupling, residual  $I-Q$  imbalance, errors in the frequency offset estimation, phase noise, and quantization. Another explanation could be the assumption of i.i.d. channel elements in the simulations.

## VI. CONCLUSIONS

An overview is given of the (changes in) signal processing, which is required to extend the physical layer of an OFDM system to multiple-input multiple-output (MIMO) OFDM. The signal processing of frame detection, time synchronization, frequency synchronization, channel estimation, synchronization tracking using pilot subcarriers, and MIMO detection algorithms is discussed. As a test case, the MIMO extension of the OFDM standard IEEE 802.11a is considered, but the results can be applied more generally. The necessary processing is not only evaluated through simulations but also by measurements using a  $3 \times 3$  MIMO test system set up in a typical office environment.

From simulations, it is concluded that the MIMO detection scheme per-antenna-coding (PAC) V-BLAST, for low SNRs, outperforms the more complex PAC soft output MLD. Moreover, the  $3 \times 3$  PAC V-BLAST achieves a comparable performance as the  $1 \times 1$  variant, even though the throughput is three times higher. Furthermore, the measurements performed with the test system [with a (partly offline) implementation of the complete signal processing] in a practical environment showed a slightly worse performance than the idealized simulation results. The explanation is that in the simulations, system degradations such as phase noise and quantization as well as propagation effects such as ill-conditioned MIMO channels are not taken into account.

Finally, measurements show that an implementation of a  $3 \times 3$  MIMO OFDM system achieves about a two times higher throughput than its  $1 \times 1$  counterpart at a given range. Two reasons can be found for not reaching the theoretical tripling of the throughput: first, mutual coupling between the branches at the transmitter and receiver side and, second, the maximum throughput enhancement by a factor of 3 can only be achieved in well-conditioned MIMO channels, i.e., having i.i.d. channel elements.

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